

# OPF Models for Power System Security Control

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- 4 Optimal Power Flow with Transient Stability Constraints
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# Research topic

- Procedures to help system operators to guarantee power system security in the context of real-time operation

# Power system security

- The ability of a power system to reach acceptable steady-state operating conditions after being subjected to sudden disturbances
- The power system should not be forced to uncontrolled cascading outages that can lead the system to a blackout

# Power system security

To reduce the risk of blackouts:

- no equipment is overloaded
- all bus voltage magnitudes are within appropriate limits
- stable operation after plausible contingencies

# Motivation

- Market clearing procedures do not explicitly consider security issues
- System operator must check system security and implement control actions if needed
  - Security assessment: state of the system under contingencies
  - Contingency filtering: identification of critical contingencies
  - Security control: design of control actions to improve the system security level

# Motivation

- Control actions → adjustments with respect to the market solution:
  - Adjustments in the generator power outputs
  - Adjustments in the demand powers
  - Adjustments in the set points of system control devices
- Security control tool → Optimal Power Flow (OPF)

# Motivation

- Market participants expect that the security control minimally modifies the market solution
- Security-constrained OPF requires:
  - To model the system behavior and stability constraints in detail
  - To deal with non-linear models and advanced stability concepts
  - To marry time-domain simulations and optimization
- Need to incorporate security constraints in the OPF problem



# Proposed procedures

OPF-based control tools to assist system operators in avoiding security problems related to:

- Voltage instability
- Small-signal instability
- Transient instability

# Proposed procedures

- Starting point → market dispatching solution adjusted by losses
- Security assessment procedures
- Contingency filtering procedures
- Security control procedures: OPF problems with stability constraints

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# Definition of voltage stability

## Voltage stability

The ability of a power system to maintain steady voltages at all buses throughout the system after suffering a disturbance from a given initial operating condition

## Voltage collapse

The process by which the sequence of events accompanying voltage instability leads to a blackout or to abnormally low voltages in a significant part of the power system

# Voltage stability analysis

System model:

$$\mathbf{g}(\mathbf{y}, \mathbf{p}) = \mathbf{0}$$

where

- $\mathbf{y}$ : algebraic variables (e.g, voltage magnitudes at load buses)
- $\mathbf{p}$ : control variables (e.g, generator power outputs)
- $\mathbf{g}$ : power flow equations

# Voltage stability analysis

## Bifurcation theory

System model:

$$\mathbf{g}(\mathbf{y}, \mathbf{p}) \rightarrow \mathbf{g}(\mathbf{y}, \mathbf{p}, \lambda)$$

where  $\lambda$  usually represents changes in system load:

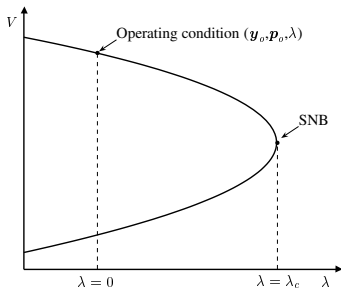
$$P_{Di} = (1 + \lambda)P_{Di}^A, \quad \forall i \in \mathcal{D}$$

$$Q_{Di} = (1 + \lambda)Q_{Di}^A, \quad \forall i \in \mathcal{D}$$

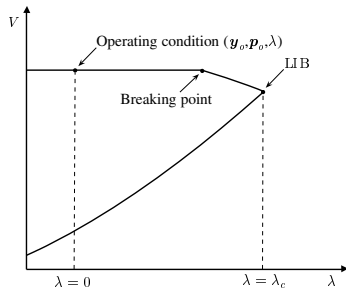
- Parameter  $\lambda$  changes “slowly”
- Voltage instability conditions:
  - Saddle-node bifurcations (SNB)
  - Limit-induced bifurcations (LIB)

# Voltage stability analysis

## Bifurcation theory



(a) Saddle-node bifurcation



(b) Limit-induced bifurcation

# Voltage stability assessment

## Loading margin

Maximum amount of additional load that the system can provide until a voltage stability limit (SNB or a critical LIB) is reached

## Loading margin $\lambda^*$

Maximum amount of additional load that the system can provide without exceeding a technical limit and ensuring that a voltage collapse does not appear within a given period of time

- Loading margin computation → Maximum loading condition problem



## Security assessment related to voltage stability

- Security assessment  $\rightarrow$  computation of the loading margin  $\lambda^*$  for post-contingency system configurations
- System operator specifies:
  - Initial set of contingencies  $\rightarrow N - 1$  criterion
  - Time period  $\Delta t$
- Loading margin  $\lambda^*$  is computed for each contingency of the initial set

# Contingency filtering related to voltage stability

- System operator specifies:
  - Security margin  $\lambda^{\text{SM}}$
- Contingency filtering criterion:
  - If  $\lambda^* \leq \lambda^{\text{SM}}$ , the contingency is selected as critical. At the loading condition defined by  $\lambda^{\text{SM}}$  the system exhibits potential voltage instability.
  - If  $\lambda^* > \lambda^{\text{SM}}$ , the contingency is filtered out

# VSC-OPF problem

## Minimize

- Cost of adjustments with respect to the base case solution

## subject to

- Power flow equations for the adjusted operating condition
- Power flow equations under stressed operating conditions
- Technical limits
- Ramping constraints

## VSC-OPF - Constraints

Power flow equations for the adjusted operating condition

- Power balance at all system buses
- Generator powers:

$$P_{Gj} = P_{Gj}^A + \Delta P_{Gj}^{\text{up}} - \Delta P_{Gj}^{\text{down}}, \quad \forall j \in \mathcal{G}$$

with

$$\Delta P_{Gj}^{\text{up}} \geq 0, \quad \forall j \in \mathcal{G}$$

$$\Delta P_{Gj}^{\text{down}} \geq 0, \quad \forall j \in \mathcal{G}$$

Superscript “A” indicates base-case solution

## VSC-OPF - Constraints

Power flow equations for the adjusted operating condition

- Demand powers:

$$P_{Di} = P_{Di}^A - \Delta P_{Di}, \quad \forall i \in \mathcal{D}$$
$$Q_{Di} = P_{Di} \tan(\psi_{Di}), \quad \forall i \in \mathcal{D}$$

with

$$\Delta P_{Di} \geq 0, \quad \forall i \in \mathcal{D}$$

Superscript “A” indicates base-case solution

## VSC-OPF - Constraints

### Power flow equations under stressed operating conditions

As many stressed operating conditions are included in the VSC-OPF problem as critical contingencies identified in the contingency filtering procedure

- Power balance at all system buses
- The line that corresponds to the critical contingency is removed
- The demand is increased according to the security margin  $\lambda^{\text{SM}}$

$$P_{Di}^s = (1 + \lambda^{\text{SM}})P_{Di} \quad \forall i \in \mathcal{D}, \quad \forall s \in \mathcal{S}$$

$$Q_{Di}^s = (1 + \lambda^{\text{SM}})P_{Di} \tan(\psi_{Di}), \quad \forall n \in \mathcal{D}, \quad \forall s \in \mathcal{S}$$

where  $P_{Di}$  corresponds to the adjusted operating condition

## VSC-OPF - Constraints

### Power flow equations under stressed operating conditions

- Generator powers:

$$P_{Gj}^s = P_{Gj} + \Delta P_{Gj}^{\text{up},s} - \Delta P_{Gj}^{\text{down},s}, \quad \forall j \in \mathcal{G}, \quad \forall s \in \mathcal{S}$$

with

$$\Delta P_{Gj}^{\text{up},s} \geq 0, \quad \forall j \in \mathcal{G}, \quad \forall s \in \mathcal{S}$$

$$\Delta P_{Gj}^{\text{down},s} \geq 0, \quad \forall j \in \mathcal{G}, \quad \forall s \in \mathcal{S}$$

where  $P_{Gj}$  corresponds to the adjusted operating condition

# VSC-OPF - Constraints

## Technical limits

For the adjusted and stressed systems:

- Maximum and minimum power output of generators
- Maximum and minimum reactive power limit of generators
- Maximum and minimum voltage magnitude at system buses
- Maximum current magnitude through system branches



# VSC-OPF - Constraints

## Ramping limits

- Ramping limits for generators:

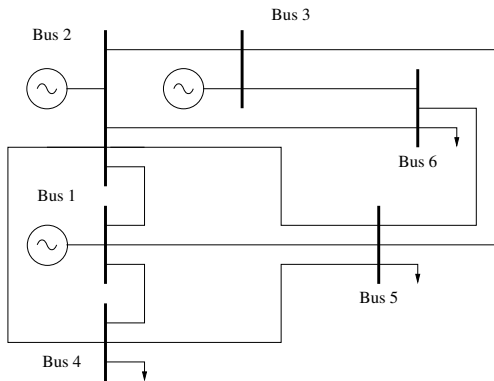
$$P_{Gj}^s - P_{Gj} \leq R_{Gj}^{\text{up}} \Delta t, \quad \forall j \in \mathcal{G}, \quad \forall s \in \mathcal{S}$$

$$P_{Gj} - P_{Gj}^s \leq R_{Gj}^{\text{down}} \Delta t, \quad \forall j \in \mathcal{G}, \quad \forall s \in \mathcal{S}$$

# Proposed redispatching procedure

- 1 - Base case operating condition:
  - Market dispatch solution adjusted by losses
- 2 - Security assessment:
  - Initial set of contingencies:  $N - 1$  contingency criterion
  - Computation of loading margins  $\lambda^*$
- 3 - Contingency filtering:
  - Comparison of loading margins  $\lambda^*$  with the required security margin  $\lambda^{\text{SM}}$
- 4 - Stressed operating conditions for the VSC-OPF problem:
  - One stressed condition per critical contingency
  - The system load is increased by  $\lambda^{\text{SM}}$  for all stressed systems
- 5 - Solve the VSC-OPF problem

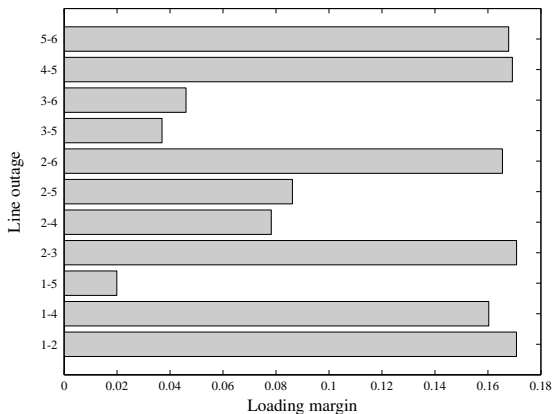
## Illustrative example: W&W 6-bus system



# Illustrative example: W&W 6-bus system

## Security assessment

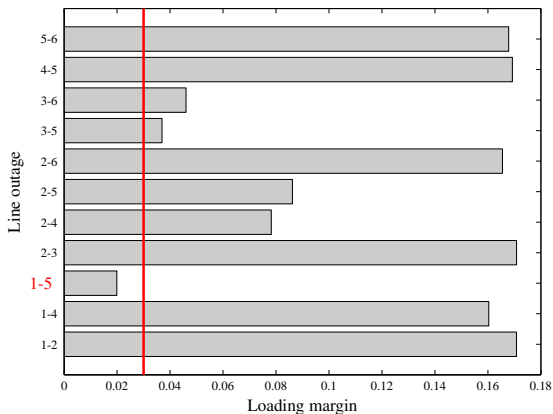
### ■ Computation of system loading margins



# Illustrative example: W&W 6-bus system

## Contingency filtering

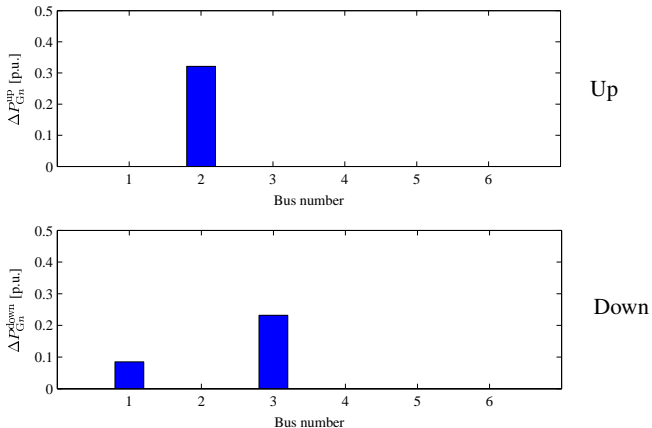
- Security margin:  $\lambda^{\text{SM}} = 0.03$



# Illustrative example: W&W 6-bus system

## Solution to the VSC-OPF problem

- Generation redispatching for  $\lambda^{\text{SM}} = 0.03$



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# Definition of small-signal stability

## Small-signal (rotor-angle) stability

The ability of a power system to maintain synchronism under small disturbances

## Undamped rotor angle oscillations

- Local mode oscillations
- Inter-area mode oscillations



## Small-signal stability analysis

System model  $\rightarrow$  DAE system:

$$\begin{bmatrix} \dot{\mathbf{x}} \\ \mathbf{0} \end{bmatrix} = \begin{bmatrix} \mathbf{f}(\mathbf{x}, \mathbf{y}, \mathbf{p}) \\ \mathbf{g}(\mathbf{x}, \mathbf{y}, \mathbf{p}) \end{bmatrix}$$

where

- $\mathbf{x}$ : state variables (e.g, machine rotor angles)
- $\mathbf{y}$ : algebraic variables (e.g, voltage magnitude at load buses)
- $\mathbf{p}$ : control variables (e.g, generator power outputs)
- $\mathbf{f}$ : equations related to state variables (e.g., synchronous machine equations)
- $\mathbf{g}$ : algebraic equations (e.g., power flow equations)

# Small-signal stability analysis

System equilibrium point:

- The system is at steady-state
- Control variables  $\mathbf{p}_o$  are known
- Remaining variables  $(\mathbf{x}_o, \mathbf{y}_o)$  are obtained by solving:

$$\begin{bmatrix} \mathbf{0} \\ \mathbf{0} \end{bmatrix} = \begin{bmatrix} \mathbf{f}(\mathbf{x}_o, \mathbf{y}_o, \mathbf{p}_o) \\ \mathbf{g}(\mathbf{x}_o, \mathbf{y}_o, \mathbf{p}_o) \end{bmatrix}$$

## Small-signal stability analysis

Linearization of DAE system at  $(\mathbf{x}_o, \mathbf{y}_o)$ :

$$\begin{bmatrix} \Delta \dot{\mathbf{x}} \\ \mathbf{0} \end{bmatrix} = \begin{bmatrix} D_x \mathbf{f} & D_y \mathbf{f} \\ D_x \mathbf{g} & D_y \mathbf{g} \end{bmatrix} \begin{bmatrix} \Delta \mathbf{x} \\ \Delta \mathbf{y} \end{bmatrix}$$

System state matrix:

$$\mathbf{A}_{\text{sys}} = D_x \mathbf{f} - D_y \mathbf{f} [D_y \mathbf{g}]^{-1} D_x \mathbf{g}$$

## Small-signal stability assessment

Eigenvalue analysis of  $\mathbf{A}_{\text{sys}}$   $\rightarrow$  Lyapunov's first method:

- If all eigenvalues of matrix  $\mathbf{A}_{\text{sys}}$  have negative real parts, the system equilibrium point is asymptotically stable
- If at least one of the eigenvalues of matrix  $\mathbf{A}_{\text{sys}}$  has a positive real part, the system equilibrium point is unstable

# Small-signal stability assessment

## Bifurcation theory

System model:

$$\begin{aligned}f(\mathbf{x}, \mathbf{y}, \mathbf{p}) &\rightarrow f(\mathbf{x}, \mathbf{y}, \mathbf{p}, \lambda) \\g(\mathbf{x}, \mathbf{y}, \mathbf{p}) &\rightarrow g(\mathbf{x}, \mathbf{y}, \mathbf{p}, \lambda)\end{aligned}$$

- Parameter  $\lambda$  changes “slowly”
- Small-signal rotor angle instability conditions:
  - Hopf bifurcations (HB)

# Small-signal stability assessment

## Bifurcation theory

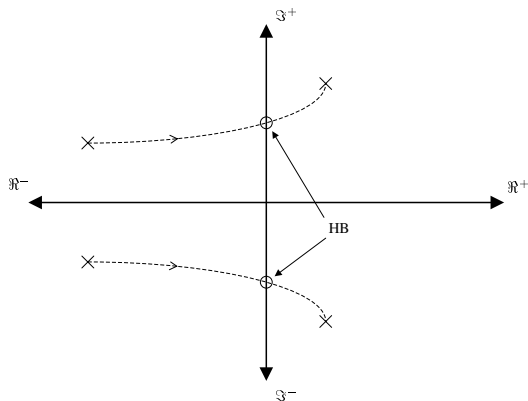


Figure : Hopf bifurcation in the complex plane

## Security assessment related to small-signal stability

- Security assessment  $\rightarrow$  computation of the loading margin  $\lambda^*$  for post-contingency system configurations + eigenvalue analysis of the state matrix for the maximum loading conditions
- System operator specifies:
  - Initial set of contingencies  $\rightarrow N - 1$  criterion
  - Time period  $\Delta t$
- Loading margin  $\lambda^*$  is computed for each contingency of the initial set
- Eigenvalue analysis is performed for the maximum loading conditions
- Critical eigenvalues  $\alpha \pm j\beta$  are calculated

# Contingency filtering related to small-signal stability

- System operator specifies:
  - Security margin  $\lambda^{\text{SM}}$
- Contingency filtering criterion:
  - If  $\lambda^* \leq \lambda^{\text{SM}}$ , the contingency is selected as critical. At the loading condition defined by  $\lambda^{\text{SM}}$  the system exhibits potential voltage instability
  - If  $\alpha > 0$ , the contingency is selected as critical. At the loading condition defined by  $\lambda^{\text{SM}}$ , the system may suffer from small-signal instability
  - If  $\lambda^* > \lambda^{\text{SM}}$  and  $\alpha < 0$ , the contingency is filtered out



# SSSC-OPF problem

## Minimize

- Cost of adjustments with respect to the base case solution

## subject to

- Power flow equations for the adjusted operating condition
- Power flow equations under stressed operating conditions
- Technical limits
- Ramping constraints
- Small-signal stability constraints

# SSSC-OPF problem

## Small-signal stability constraints

- First order Taylor series expansion of  $\alpha^s (P_G^s)$
- Resulting constraint:

$$\alpha^s + F^s \sum_{j \in \mathcal{G}} \left. \frac{\partial \alpha^s}{\partial P_{Gj}^s} \right|_u (P_{Gj}^s - P_{Gj}^{s,u}) \leq \alpha^{\max}, \quad \forall s \in \mathcal{S}_u$$

where:

- $\alpha^s$ : actual value of the real part of the critical eigenvalue
- $\left. \frac{\partial \alpha^s}{\partial P_{Gj}^s} \right|_u$ : sensitivity of  $\alpha^s$  with respect to  $P_{Gj}^s$
- $F^s$ : scaling factor introduced to limit the size of  $(P_{Gj}^s - P_{Gj}^{s,u})$
- $\alpha^{\max}$ : upper limit for the real part of the critical eigenvalue

# SSSC-OPF problem

## Small-signal stability constraints

- The variations in generator powers must be always consistent with the signs of the sensitivities:

$$P_{Gj}^s - P_{Gj}^{s,u} \geq 0 \quad \text{if} \quad \frac{\partial \alpha^s}{\partial P_{Gj}^s} < 0, \quad \forall j \in \mathcal{G}, \quad \forall s \in \mathcal{S}_u$$

$$P_{Gj}^s - P_{Gj}^{s,u} \leq 0 \quad \text{if} \quad \frac{\partial \alpha^s}{\partial P_{Gj}^s} > 0, \quad \forall j \in \mathcal{G}, \quad \forall s \in \mathcal{S}_u$$

# Proposed redispatching procedure

- 1 - Base case operating condition:
  - Market dispatch solution adjusted by losses
- 2 - Security assessment:
  - Initial set of contingencies:  $N - 1$  contingency criterion
  - Computation of loading margins  $\lambda^*$
  - Eigenvalue analysis at the maximum loading condition
- 3 - Contingency filtering:
  - Comparison of loading margins  $\lambda^*$  with the require security margin  $\lambda^{\text{SM}}$
  - Inspection of critical eigenvalues
- 4 - Stressed operating conditions for the SSSC-OPF problem:
  - One stressed condition per critical contingency
  - The system load is increased by  $\lambda^{\text{SM}}$  for all stressed systems

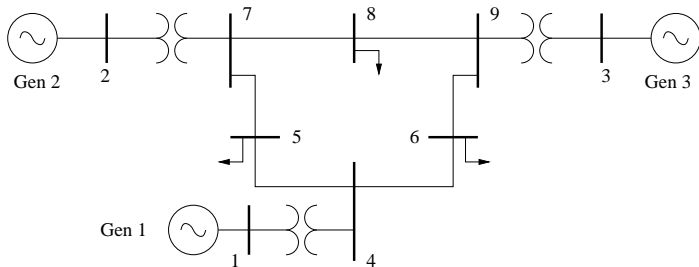
## Proposed redispatching procedure

5 - Solve the SSSC-OPF problem

6 - Checking the solution:

- Eigenvalue analysis of the stressed operating conditions
- If one or more stressed conditions show small-signal instability:
  - Sensitivity computation
  - Small-signal stability constraints are incorporated to the SSSC-OPF problem
  - The procedure continues in step 5
- If all stressed conditions are stable the procedure stops

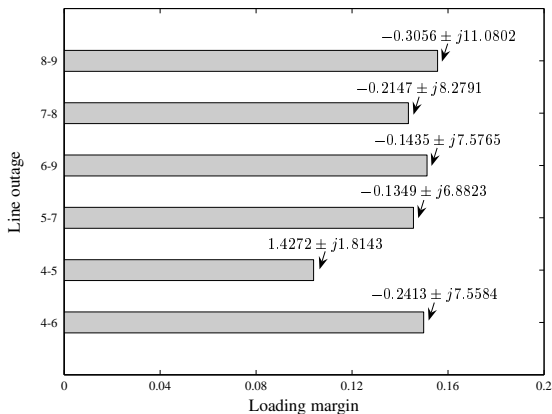
## Illustrative example: WECC 9-bus, 3-machine system



# Illustrative example: WECC 9-bus, 3-machine system

## Security assessment

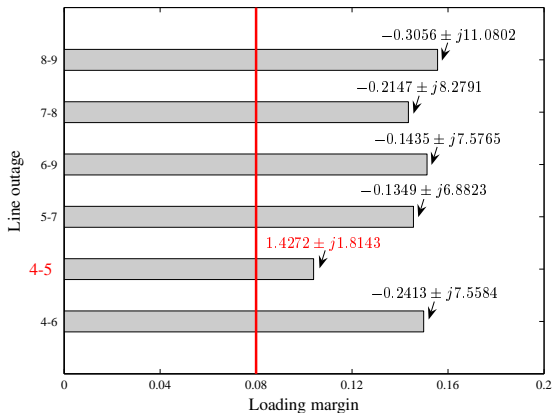
- Computation of system loading margins + eigenvalue analysis



# Illustrative example: WECC 9-bus, 3-machine system

## Contingency filtering

- Security margin:  $\lambda^{\text{SM}} = 0.08$





# Illustrative example: WECC 9-bus, 3-machine system

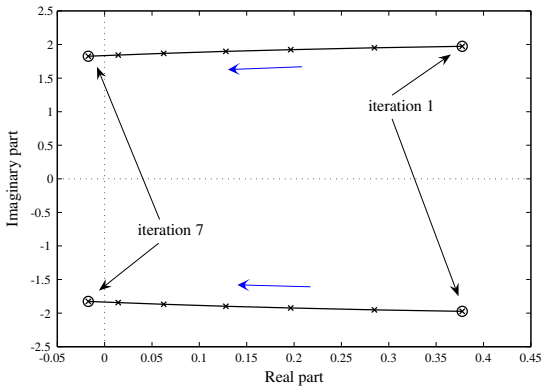
## First iteration of the procedure

- The stressed condition exhibits small-signal instability:
  - Critical eigenvalue =  $0.3775 \pm j1.9729$
- Sensitivities are computed
- Small-signal stability constraints are incorporated into the OPF problem
- SSSC-OPF problem is solved again

# Illustrative example: WECC 9-bus, 3-machine system

## Procedure iterations

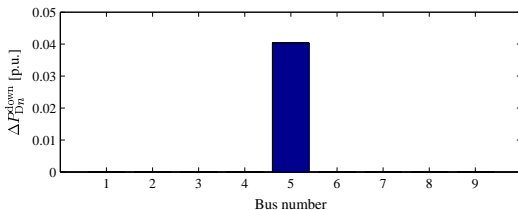
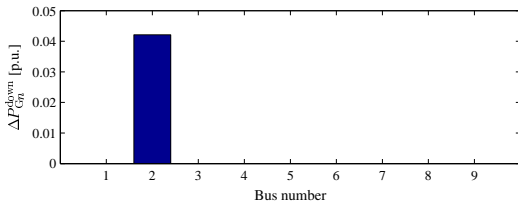
- Evolution of the critical eigenvalue in the complex plain



# Illustrative example: WECC 9-bus, 3-machine system

## Procedure solution

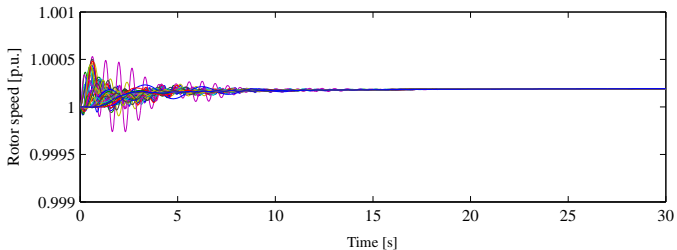
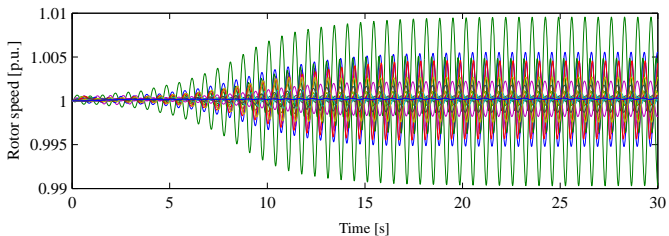
### ■ Redispatching actions



## Case study: IEEE 145-bus, 50-machine system

- Security assessment: 434 contingencies analyzed
- Contingency filtering for  $\lambda^{\text{SM}} = 0.05$ :
  - Two contingencies selected due to voltage stability issues
  - Three contingencies selected due to small-signal stability issues
- SSSC-OPF problem includes five stressed operating conditions
- First iteration:
  - Only one stressed operating condition shows small-signal instability for  $\lambda^{\text{SM}} = 0.05$
- Solution attained after nine iterations:
  - Generator redispatching + load curtailment

## Case study: IEEE 145-bus, 50-machine system



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# Definition of transient stability

## Transient stability

The ability of a power system to maintain synchronism after large disturbances

## Loss of synchronism

- Aperiodic angular separation of the system machines
  - First-swing instability
  - Multi-swing instability

# Transient stability analysis

## System model

DAE system:

$$\begin{bmatrix} \dot{\mathbf{x}} \\ \mathbf{0} \end{bmatrix} = \begin{bmatrix} \mathbf{f}(\mathbf{x}, \mathbf{y}, \mathbf{p}) \\ \mathbf{g}(\mathbf{x}, \mathbf{y}, \mathbf{p}) \end{bmatrix}$$

where

- $\mathbf{x}$ : state variables (e.g, machine rotor angles)
- $\mathbf{y}$ : algebraic variables (e.g, voltage magnitudes at load buses)
- $\mathbf{p}$ : control variables (e.g, generator power outputs)
- $\mathbf{f}$ : equations related to state variables (e.g., synchronous machine equations)
- $\mathbf{g}$ : algebraic equations (e.g., power flow equations)



# Transient stability assessment

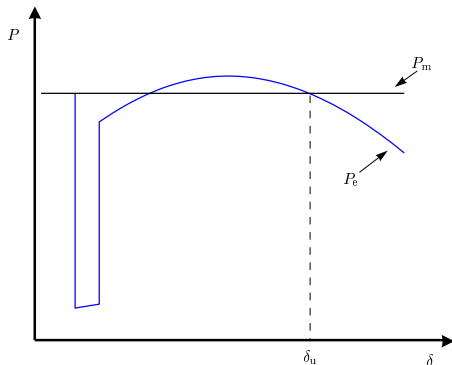
## SIME method

- Combines the time-domain simulation and the Equal-Area Criterion (EAC)
- Identifies the separation pattern of the system machines:
  - Group of critical machines
  - Group of non-critical machines
- One-Machine Infinite Bus (OMIB) equivalent system
- Stability of the OMIB equivalent system is checked by using the EAC

# Transient stability assessment

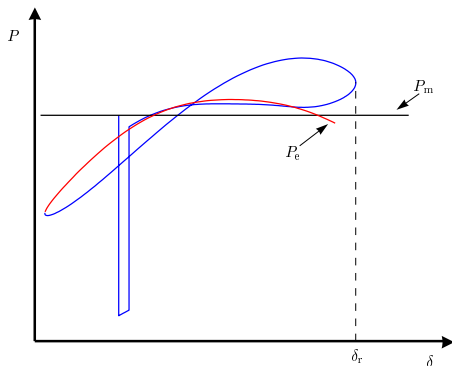
## SIME method

- First-swing unstable case



# Transient stability assessment SIME method

## ■ Multi-swing unstable case



## Security assessment related to transient stability

- Initial set of contingencies  $\rightarrow N - 1$  criterion
- Contingencies analyzed:
  - Three-phase-to-ground symmetrical fault and the subsequent fault clearing by tripping the corresponding line
- Time-domain simulation complemented by the SIME method

# Contingency filtering related to transient stability

- Contingency filtering criterion:
  - Either the system exhibits first-swing or multi-swing instability the contingency is selected
- If the system presents first-swing instability:
  - The SIME method provides the OMIB equivalent and the unstable angle  $\delta_u$
- If the system presents multi-swing instability:
  - The SIME method provides the OMIB equivalent and the return angle  $\delta_r$  in the first-swing

# TSC-OPF problem

## Minimize

- Cost of adjustments with respect to the base case solution

## subject to

- Power flow equations for the adjusted operating condition
- Technical limits
- Transient stability constraints

## Transient stability constraints

- Discrete-time equations of the multi-machine system:

$$\delta_j^{t+1} - \delta_j^t - \frac{t_{\text{step}}}{2} \omega_b (\omega_j^{t+1} - 1 + \omega_j^t - 1) = 0, \quad \forall t \in \mathcal{T}$$

$$\omega_j^{t+1} - \omega_j^t - \frac{t_{\text{step}}}{2} \frac{1}{M_j} (P_{mj}^{t+1} - P_{ej}^{t+1} + P_{mj}^t - P_{ej}^t) = 0, \quad \forall t \in \mathcal{T}$$

## Transient stability constraints

- OMIB rotor angle:

$$\delta_{\text{OMIB}}^t = \frac{1}{M_{\text{C}}} \sum_{j \in \mathcal{G}_{\text{C}}} M_j \delta_j^t - \frac{1}{M_{\text{NC}}} \sum_{j \in \mathcal{G}_{\text{NC}}} M_j \delta_j^t, \quad \forall t \in \mathcal{T}$$

- Limit on the OMIB rotor angle:

$$\delta_{\text{OMIB}}^t \leq \delta_{\text{OMIB}}^{\max}, \quad \forall t \in \mathcal{T}$$



# Proposed redispatching procedure

- 1 - Base case operating condition
- 2 - Security assessment:
  - Initial set of contingencies:  $N - 1$  contingency criterion
  - Time-domain simulation complemented by the SIME method
- 3 - Contingency filtering:
  - First-swing and multi-swing instability contingencies
- 4 - Transient stability constraints:
  - For first-swing instability  $\rightarrow \delta_{\text{OMIB}}^{\text{max}} = \delta_u$
  - For multi-swing instability  $\rightarrow \delta_{\text{OMIB}}^{\text{max}} = \delta_r - \Delta\delta$

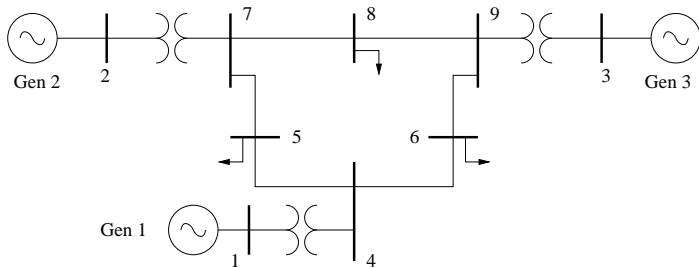
# Proposed redispatching procedure

5 - Solve the TSC-OPF problem

6 - Checking the solution:

- Time-domain simulation complemented by the SIME method
- If one or more contingencies show transient instability:
  - Updating  $\delta_{OMIB}^{\max}$
  - The procedure continues in step 5
- If all contingencies are stable the procedure stops

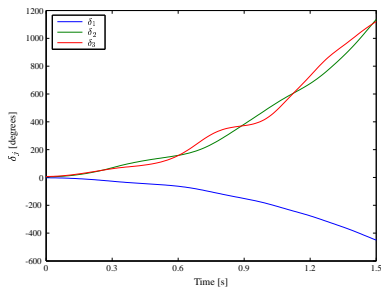
## Illustrative example: WECC 9-bus, 3-machine system



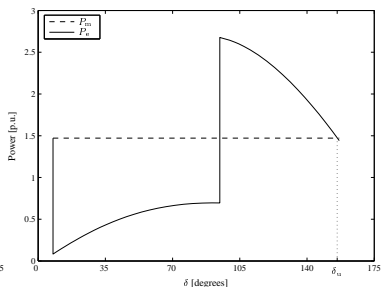
# Illustrative example: WECC 9-bus, 3-machine system

## Security assessment

- Fault at bus 7, cleared after 0.3 s by tripping the line 7-5
- First-swing instability  $\rightarrow \delta_u = 155.01$  degrees



(a) Rotor angle trajectories

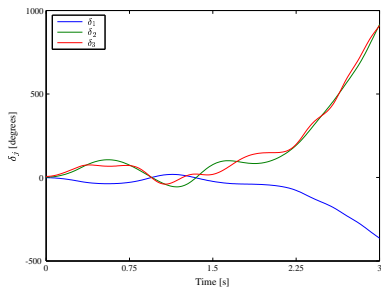


(b) OMIB plot

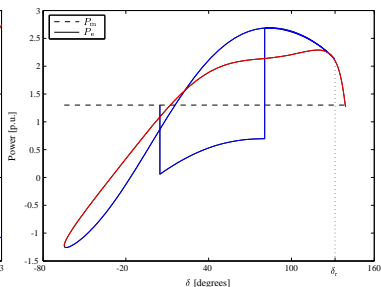
# Illustrative example: WECC 9-bus, 3-machine system

## Procedure iterations

- First iteration
- Multi-swing instability  $\rightarrow \delta_r = 131.11$  degrees



(c) Rotor angle trajectories

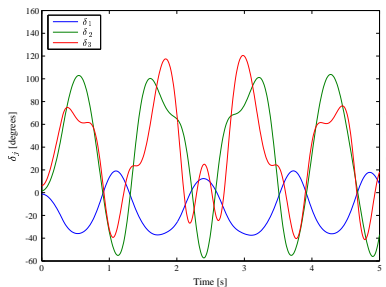


(d) OMIB plot

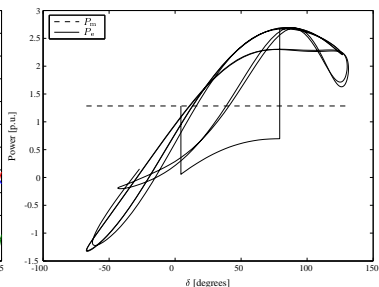
# Illustrative example: WECC 9-bus, 3-machine system

## Procedure iterations

- Second and final iteration
- The system is stable



(e) Rotor angle trajectories

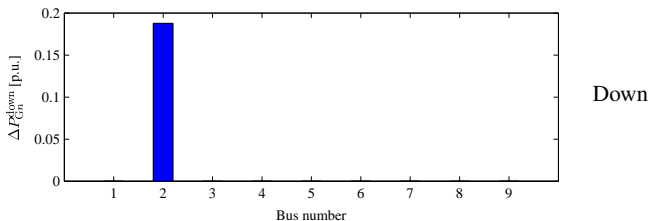
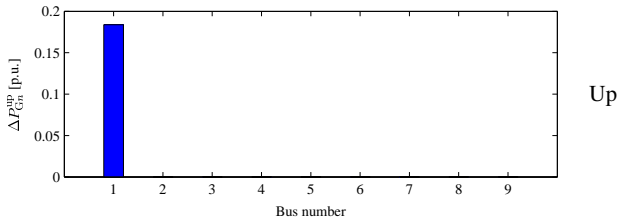


(f) OMIB plot

# Illustrative example: WECC 9-bus, 3-machine system

## Procedure solution

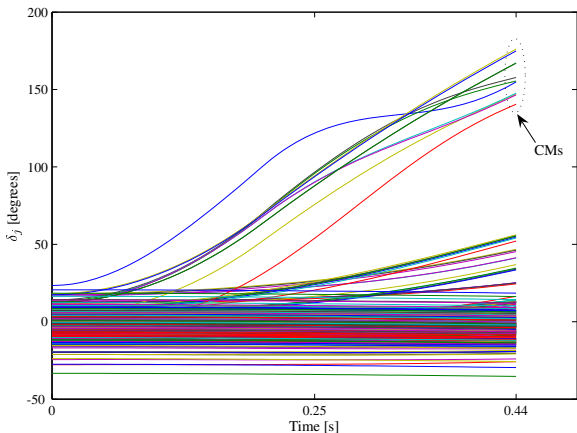
### ■ Redispatching actions:



# Case study: Real-world 1228-bus, 292-machine system

## Security assessment

- Fault at a bus, cleared after 0.2 s
- First-swing instability  $\rightarrow \delta_{\text{u}} = 157.75$  degrees

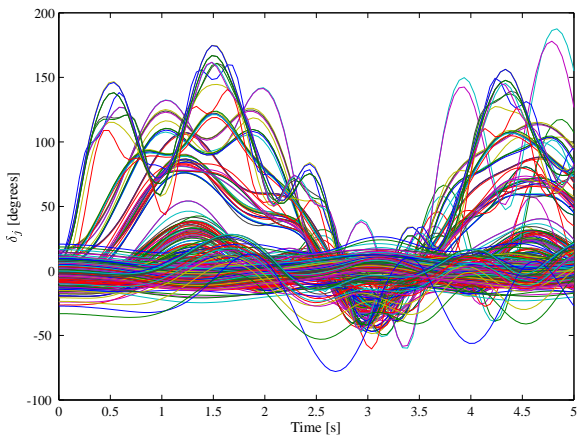




# Case study: Real-world 1228-bus, 292-machine system

## First and final iteration

- The system is stable after generation redispatching



# Index

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- 2 Optimal Power Flow with Voltage Stability Constraints
- 3 Optimal Power Flow with Small-Signal Stability Constraints
- 4 Optimal Power Flow with Transient Stability Constraints
- 5 Contributions and Ongoing Research Work**

## Contributions

- 1 - R. Zárate-Miñano, A. J. Conejo and F. Milano, “OPF-based security redispatching including FACTS devices”, *IET Generation Transmission & Distribution*.
- 2 - R. Zárate-Miñano, T. Van Cutsem, F. Milano and A. J. Conejo, “Securing transient stability using time-domain simulations within and optimal power flow”, *IEEE Transactions on Power Systems*.
- 3 - R. Zárate-Miñano, F. Milano and A. J. Conejo, “An OPF methodology to ensure small-signal stability”, *IEEE Transactions on Power Systems*.

# Ongoing research

- Impact of renewable generation on power system security
  - Modeling of stochastic perturbations in power systems
    - Stochastic differential-algebraic equations (SDAE)
  - Stability of power systems with an important penetration of renewable generation
    - Stability of power systems modeled as SDAE